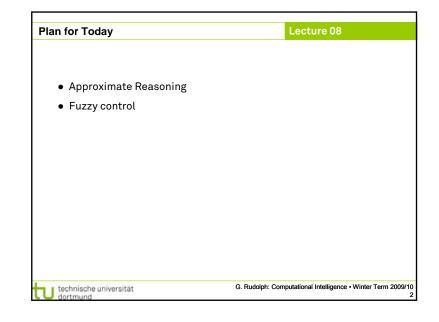
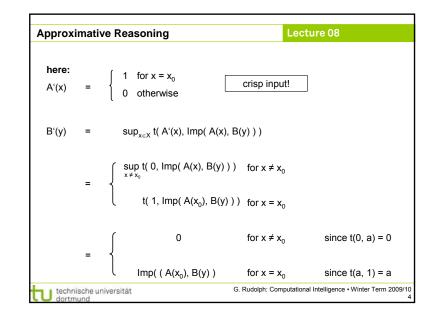
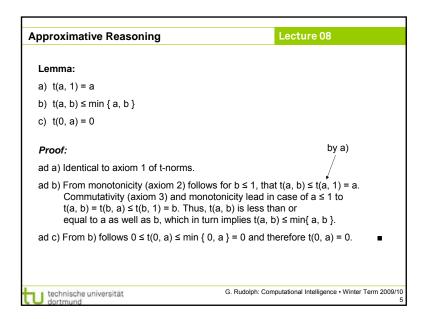
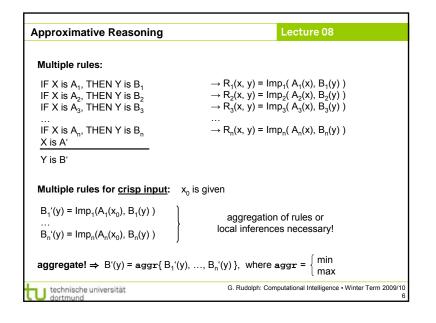
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Computational Intelligence Winter Term 2009/10	
Prof. Dr. Günter Rudolph Lehrstuhl für Algorithm Engineering (LS 11) Fakultät für Informatik	
TU Dortmund	



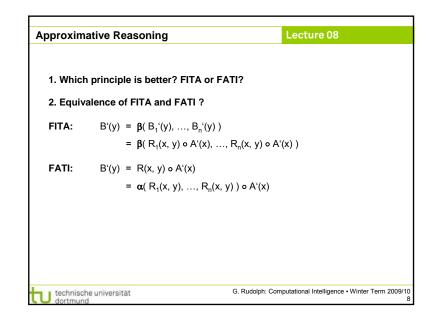
pproximative Reasoning	Lecture 08
So far:	
• p: IF X is A THEN Y is B	
$\rightarrow R(x, y) = Imp(A(x), B(y))$	rule as relation; fuzzy implication
• rule: IF X is A THEN Y is B fact: X is A' conclusion: Y is B'	
$\rightarrow B^{t}(y) = sup_{x \in X} \: t(\: A^{t}(x), \: R(x, \: y) \:)$	composition rule of inference
Thus:	
• B'(y) = sup <sub>x \in X</sub> t( A'(x), Imp( A(x), B(y) ) )	)
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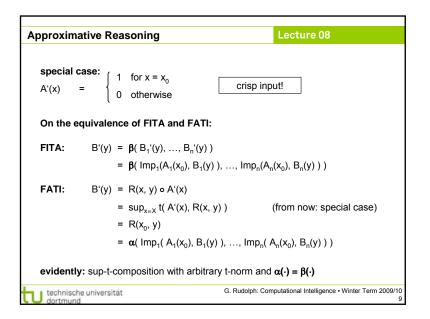




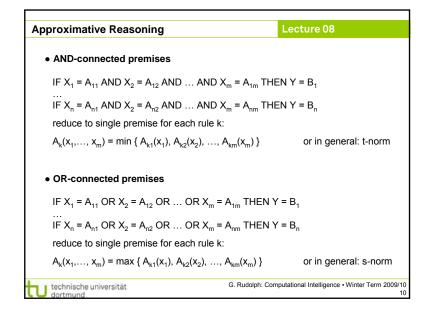


App	proximative Reasoning	Lecture 08
<u>FI</u>	TA: "First inference, then aggregate!"	-
1.	Each rule of the form IF $X$ is $A_k$ THE an appropriate fuzzy implication Imp $R_k(x, y) = Imp_k(A_k(x), B_k(y))$ .	
2.	Determine $B_k'(y) = R_k(x, y) \circ A'(x)$ for	r all k = 1,, n (locale inference).
3.	Aggregate to $B'(y) = \beta(B_1'(y),, B_1)$	"'(y) ).
	<b>TI:</b> "First aggregate, then inference!" Each rule of the form IF X ist $A_k$ THE an appropriate fuzzy implication Imp $R_k(x, y) = Imp_k(A_k(x), B_k(y))$ .	EN Y ist B <sub>k</sub> must be transformed by
2.	Aggregate $R_1,, R_n$ to a superrela $R(x, y) = \alpha(R_1(x, y),, R_n(x, y)).$	tion with aggregating function $\alpha(\cdot)$ :
3.	Determine $B'(y) = R(x, y) \circ A'(x) w.r$	t. superrelation (inference).
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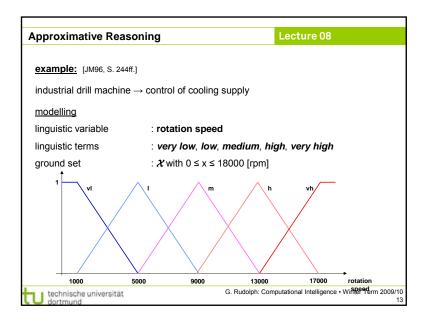




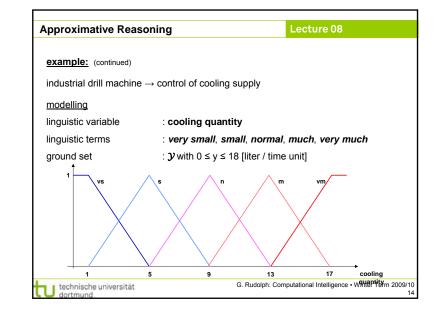
Approximative Reasoning		Lecture 08
important:		
• if rules of the form IF X is A THEN	Y is B interpreted	d as logical implication
$\Rightarrow R(x, y) = Imp(A(x), B(y)) make$	es sense	
• we obtain: $B'(y) = \sup_{x \in X} t(A'(x), F$	R(x, y) )	
$\Rightarrow$ the worse the match of premise A	(x), the larger is t	he fuzzy set B'(y)
$\Rightarrow$ follows immediately from axiom 1:	$a \le b$ implies Imp	$p(a, z) \ge Imp(b, z)$
interpretation of output set B'(y):		
<ul> <li>B'(y) is the set of values that are st</li> </ul>	till possible	
each rule leads to an additional res	striction of the valu	ues that are still possible
$\Rightarrow$ resulting fuzzy sets B <sup><math>\cdot</math></sup> <sub>k</sub> (y) obtained	d from single rules	s must be mutually intersected!
$\Rightarrow$ aggregation via B'(y) = min { B <sub>1</sub>	ʻ(y),, B <sub>n</sub> ʻ(y) }	
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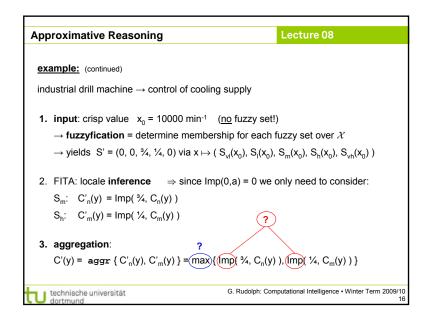


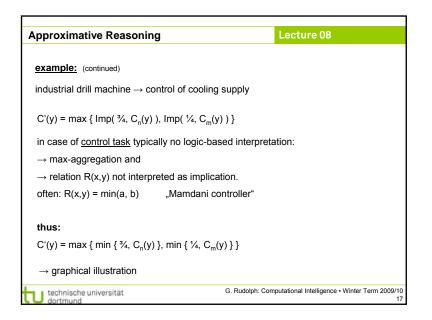
pproximative Reasoning	Lecture 08
important:	
• if rules of the form IF X is A THEN Y is implications, then the function Fct(·) in	<b>B</b> are <u>not</u> interpreted as <u>logical</u>
R(x, y) = Fct(A)	(x), B(y) )
can be chosen as required for desired i	nterpretation.
• frequent choice (especially in fuzzy con	itrol):
- R(x, y) = min { A(x), B(x) }	Mamdami – "implication"
$- R(x, y) = A(x) \cdot B(x)$	Larsen – "implication"
$\Rightarrow$ of course, they are no implications but	t special t-norms!
$\Rightarrow$ thus, if <u>relation R(x, y) is given</u> , then the <i>composition rule of inference</i>	
$B'(y) = A'(x) \circ R(x, y) = sup$	o <sub>x∈X</sub> min { A'(x), R(x, y) }
still can lead to a conclusion via fuzzy	logic.
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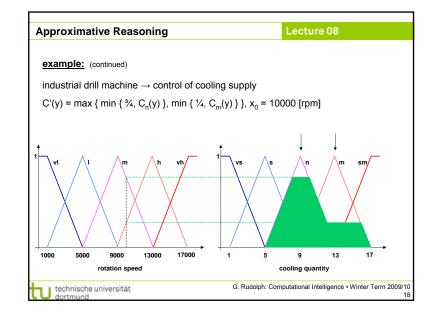


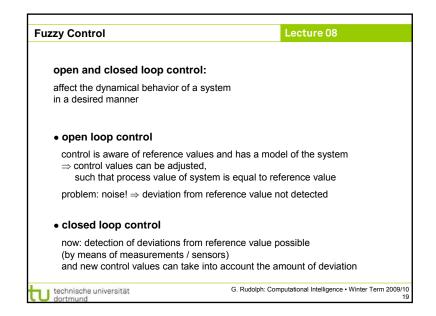
Approximative Rea	soning		Lecture 08	
example: (continued)				
industrial drill machin	$e \rightarrow control of cooling$	g supply		
rule base				
IF rotation speed I	s very low then coo	oling quantity	IS very small	
	low		small	
	medium		normal	
	high		much	
	very high		very much	
	ţ		Ţ	
sets	$S_{vl}, S_l, S_m, S_h, S_{vh}$	sets	$C_{vs}, C_s, C_n, C_m, C$	vm
	rotation <u>speed</u> "	" <u>c</u>	cooling quantity"	
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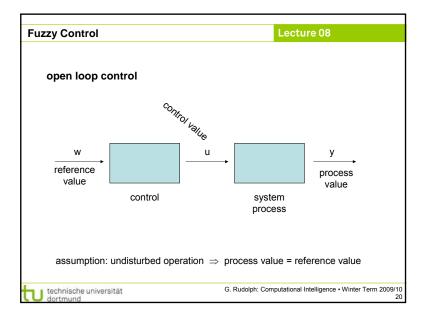


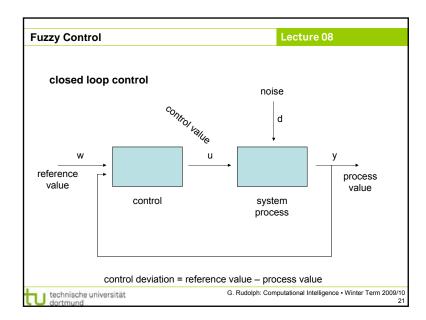




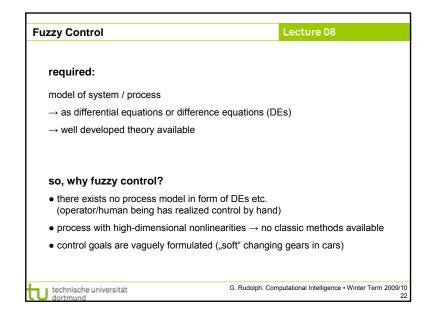


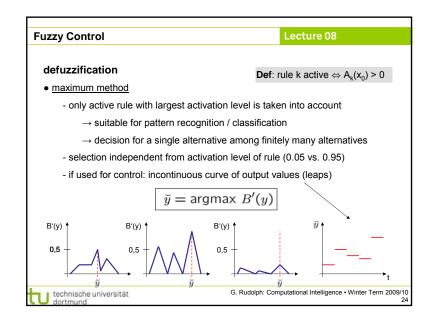


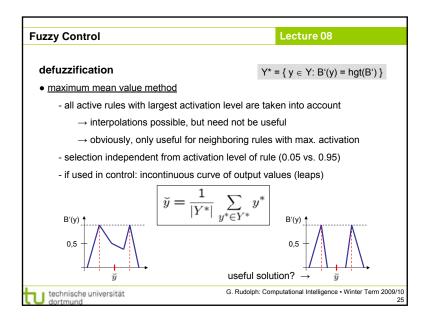




uzzy Control		Lecture 08
fuzzy description of contro	l behav	ior
IF X is $A_1$ , THEN Y is $B_1$ IF X is $A_2$ , THEN Y is $B_2$ IF X is $A_3$ , THEN Y is $B_3$  IF X is $A_n$ , THEN Y is $B_n$ X is A'		similar to approximative reasoning
Y is B'	J	
but fact A' is not a fuzzy set	but a cri	isp input
$\rightarrow$ actually, it is the current p	rocess	value
fuzzy controller executes info $\rightarrow$ yields fuzzy output set B'		step
but crisp control value requir	ed for th	ne process / system
$\rightarrow$ defuzzification (= "conder	nse" fuzz	zy set to crisp value)
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uzzy Control	Lecture 08
defuzzification	
Center of Gravity (COG)	
- all active rules are taken into acco	unt
ightarrow but numerically expensive	only valid for HW solution, today!
ightarrow borders cannot appear in ou	tput(∃ work-around)
- if only single active rule: independe	ent from activation level
- continuous curve for output values	
$\check{y} = \frac{\int y \cdot B}{\int B'(z)}$	$\frac{y'(y)dy}{y)dy}$
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