

Computational Intelligence Winter Term 2011/12

Lehrstuhl für Algorithm Engineering (LS 11)

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(known)

Application Fields of ANNs

Classification

given: set of training patterns (input / output)

(unknown)

input

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parameters $f(x; (\tilde{x}_1, \tilde{y}_1), \ldots, (\tilde{x}_m, \tilde{y}_m), w_1, \ldots, w_n) \rightarrow \hat{y}$ training patterns

 \tilde{x}_i

weights (learnt)

phase I: train network

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(e.g. class A, class B, ...)

output = label

output

(guessed)

phase II: apply network to unkown inputs for classification

Recurrent MLP

Plan for Today

Jordan Nets ■ technische universität

time series x_1 , x_2 , x_3 , ...

training patterns:

■ Flman Nets

Application Fields of ANNs

■ Function Approximation

• Radial Basis Function Nets (RBF Nets)

 Classification Prediction

Model Training

Application Fields of ANNs

Prediction of Time Series

(e.g. temperatures, exchange rates, ...) task: given a subset of historical data, predict the future

predictor

 $f(x_{t-k}, x_{t-k+1}, \dots, x_t; w_1, \dots, w_n) \to \hat{x}_{t+\tau}$

historical data where true output is known;

apply network to historical inputs for

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predicting unkown outputs

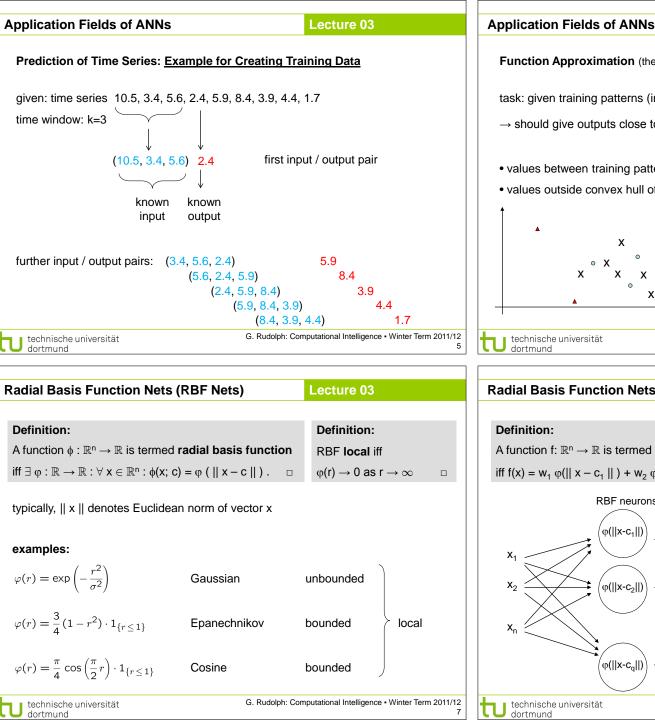
phase I:

phase II:

train network

error per pattern = $(\hat{x}_{t+\tau} - x_{t+\tau})^2$

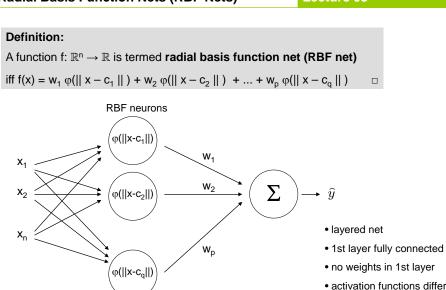
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task: given training patterns (input / output), approximate unkown function → should give outputs close to true unknown function for arbitrary inputs values between training patterns are interpolated • values outside convex hull of training patterns are extrapolated x: input training pattern : input pattern where output to be interpolated ▲: input pattern where output to be extrapolated technische universität G. Rudolph: Computational Intelligence • Winter Term 2011/12 **Radial Basis Function Nets (RBF Nets)** Lecture 03 **Definition:**

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Function Approximation (the general case)



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Radial Basis Function Nets (RBF Nets) Lecture 03 given : N training patterns (x_i, y_i) and q RBF neurons : weights w₁, ..., w_a with minimal error find solution: we know that $f(x_i) = y_i$ for i = 1, ..., N or equivalently $\sum_{k=1}^{q} w_k \cdot \varphi(\|x_i - c_k\|) = y_i$ known value known value $\Rightarrow \sum_{k=1}^{q} w_k \cdot p_{ik} = y_i$ \Rightarrow N linear equations with q unknowns G. Rudolph: Computational Intelligence • Winter Term 2011/12 technische universität Radial Basis Function Nets (RBF Nets) Lecture 03 complexity (naive) $W = (P'P)^{-1} P' y$ P'P: N2 q inversion: q3 P'y: qN multiplication: q² $O(N^2 q)$ **remark:** if N large then inaccuracies for P'P likely ⇒ first analytic solution, then gradient descent starting from this solution requires differentiable basis functions! G. Rudolph: Computational Intelligence • Winter Term 2011/12 ■ technische universität

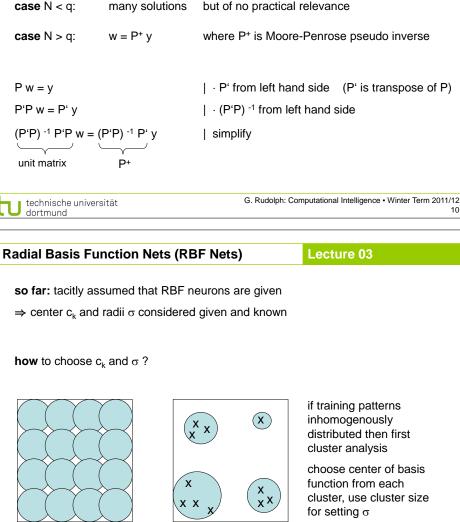
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Radial Basis Function Nets (RBF Nets)

 $W = P^{-1} y$

in matrix form: P w = y

case N = q:



if P has full rank

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with $P = (p_{ik})$ and $P: N \times q, y: N \times 1, w: q \times 1,$

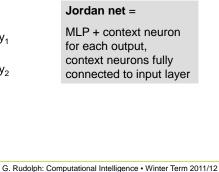
advantages: additional training patterns → only local adjustment of weights optimal weights determinable in polynomial time • regions not supported by RBF net can be identified by zero outputs disadvantages: • number of neurons increases exponentially with input dimension • unable to extrapolate (since there are no centers and RBFs are local) G. Rudolph: Computational Intelligence • Winter Term 2011/12 technische universität **Recurrent MLPs** Lecture 03 Elman nets (1990) Elman net = MLP + context neuron for each neuron output of MLP, context neurons fully connected to associated MLP layer

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Radial Basis Function Nets (RBF Nets)

Jordan nets (1986) context neuron: reads output from some neuron at step t and feeds value into net at step t+1 technische universität dortmund **Recurrent MLPs** Training?

Recurrent MLPs



Lecture 03

Lecture 03

but reasonable if most recent past more important than layers far away

- ⇒ unfolding in time ("loop unrolling")
- identical MLPs serially connected (finitely often)
- results in a large MLP with many hidden (inner) layers
- backpropagation may take a long time

Why using backpropagation?

⇒ use Evolutionary Algorithms directly on recurrent MLP!



13

15