

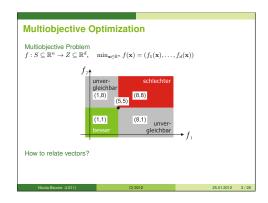
Computational Intelligence

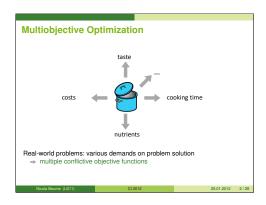
Winter Term 2012/13

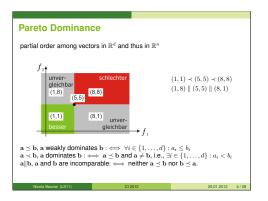
Prof. Dr. Günter Rudolph Lehrstuhl für Algorithm Engineering (LS 11)

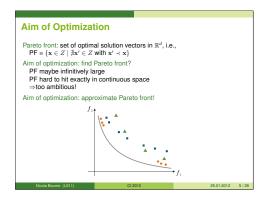
Dr. Nicola Beume

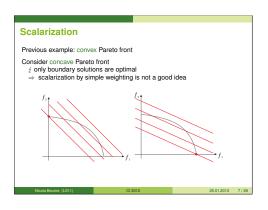
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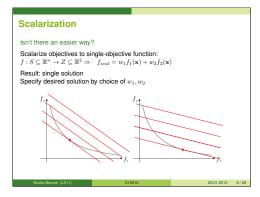








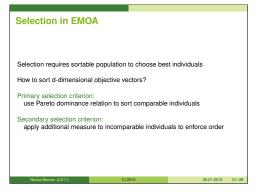


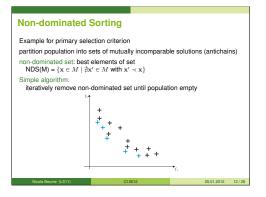


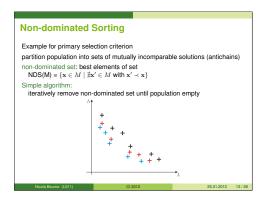


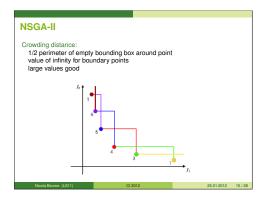
Evolutionary Algorithms Evolutionary Multiobjective Optimization Algorithms (EMOA) Multiobjective Optimization Evolutionary Algorithms (MOEA) **variation** **variation

Non-dominated Sorting Example for primary selection criterion partition population into sets of mutually incomparable solutions (antichains) non-dominated set: best elements of set NDS(M) = $\{x \in M \mid \frac{1}{T}x' \in M \text{ with } x' \prec x\}$ Simple algorithm: iteratively remove non-dominated set until population empty





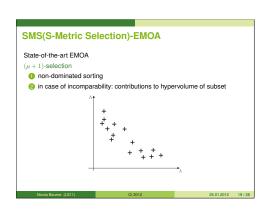


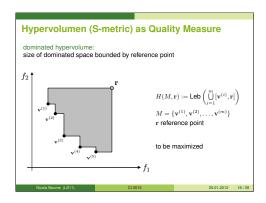


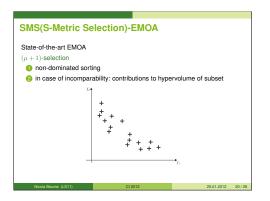
NSGA-II Popular EMOA: Non-dominated Sorting Genetic Algorithm II $(\mu + \mu)$ -selection: • perform non-dominated sorting on all $\mu + \mu$ individuals • take best subsets as long as they can be included completely • if population size μ not reached but next subset does not fit in completely: apply secondary selection criterion *crowding distance* to that subset • fill up population with best ones w.r.t. the *crowding distance*

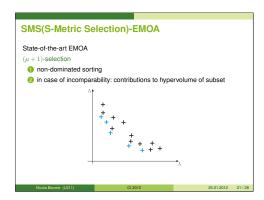
imagine point in the middle of the search space d=2:1/4 better, 1/4 worse, 1/2 incomparable d=3:1/8 better, 1/8 worse, 1/2 incomparable d=3:1/8 better, 1/8 worse, 3/4 incomparable general: fraction 2^{-d+1} comparable, decreases exponentially ⇒typical case: all individuals incomparable ⇒mainly secondary selection criterion in operation Drawback of crowding distance: rewards spreading of points, does not reward approaching the Pareto front ⇒NSGA-II diverges for large d, difficulties already for d=3

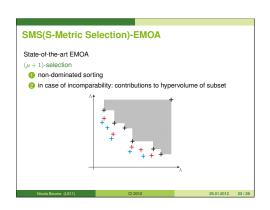
Difficulties of Selection Secondary selection criterion has to be meaningful! Desired: choose best subset of size μ from individuals How to compare sets of partially incomparable points? ⇒ use quality indicators for sets One approach for selection ⇒for each point: determine contribution to quality value of set ⇒sort points according to contribution

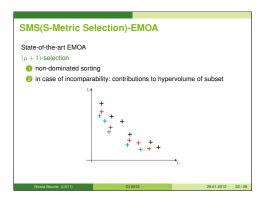


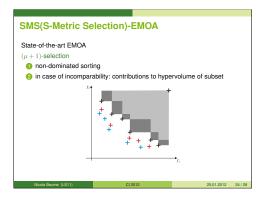


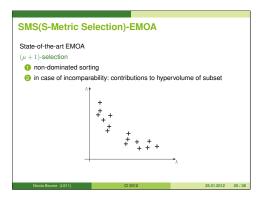












Conclusions on EMOA

NSGA-II

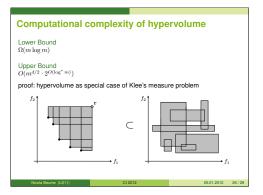
only suitable in case of d=2 objective functions otherwise no convergence to Pareto front

SMS-EMOA

also effective for d > 2 due to hypervolume hypervolume calculation time-consuming ⇒use approximation of hypervolume

Other state-of-the-art EMOA, e.g.

- MO-CMA-ES: CMA-ES + hypervolume selection
- ε-MOEA: objective space partitioned into grid, only 1 point per cell
- . MSOPS: selection acc. to ranks of different scalarizations



Conclusions

- · real-world problems are often multiobjective
- Pareto dominance only a partial order
- a priory: parameterization difficult
- a posteriori: choose solution after knowing possible compromises
- · state-of-the-art a posteriori methods: EMOA, MOEA
- EMOA require sortable population for selection
- use quality measures as secondary selection criterion
- hypervolume: excellent quality measure, but computationally intensive
- use state-of-the-art EMOA, other may fail completely

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