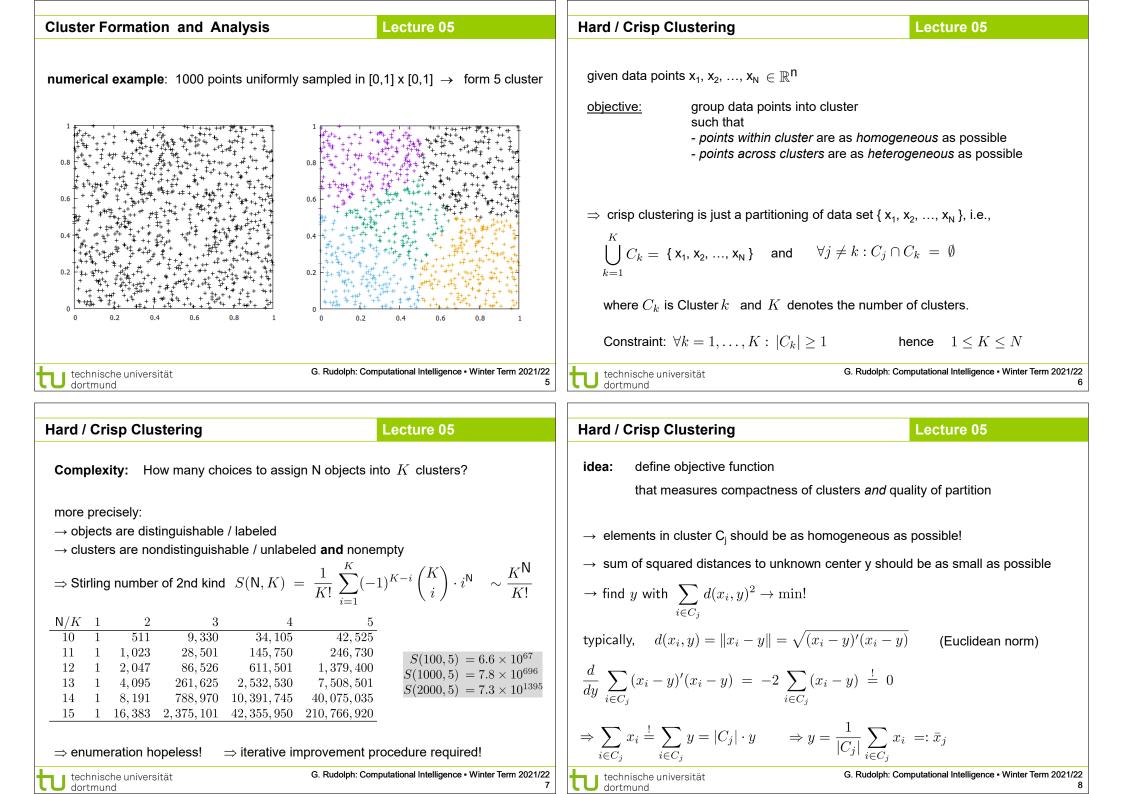
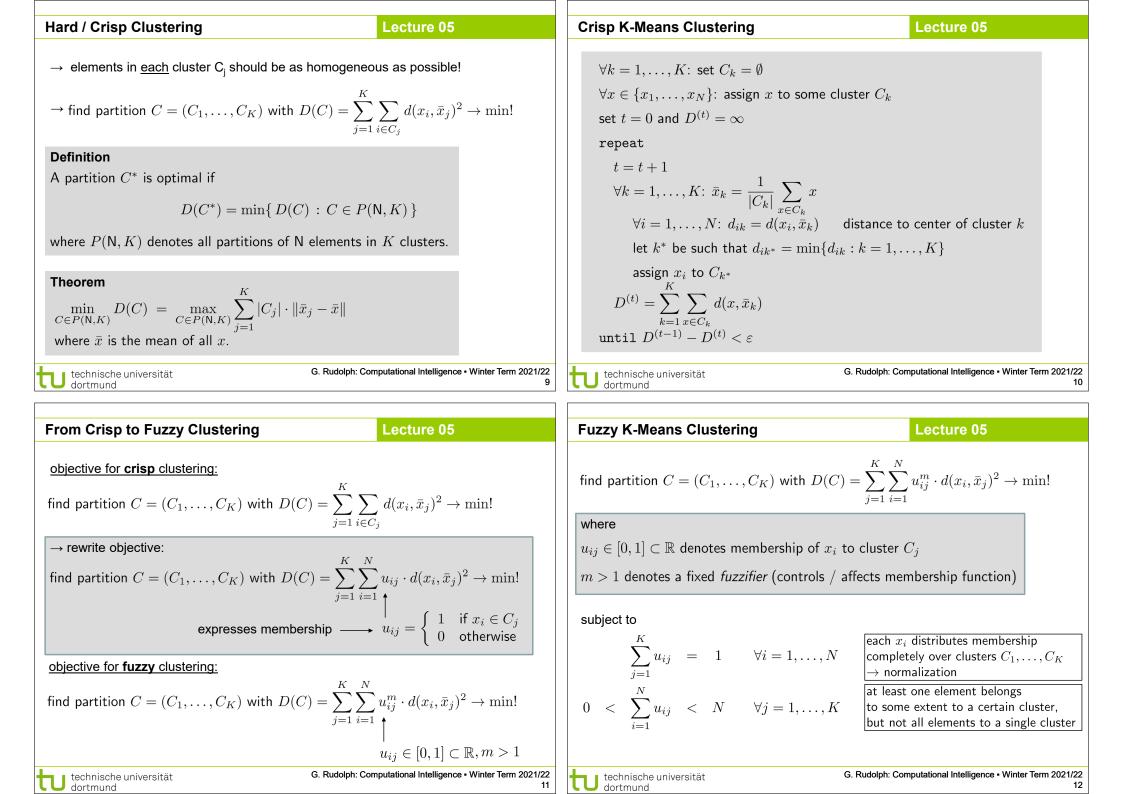
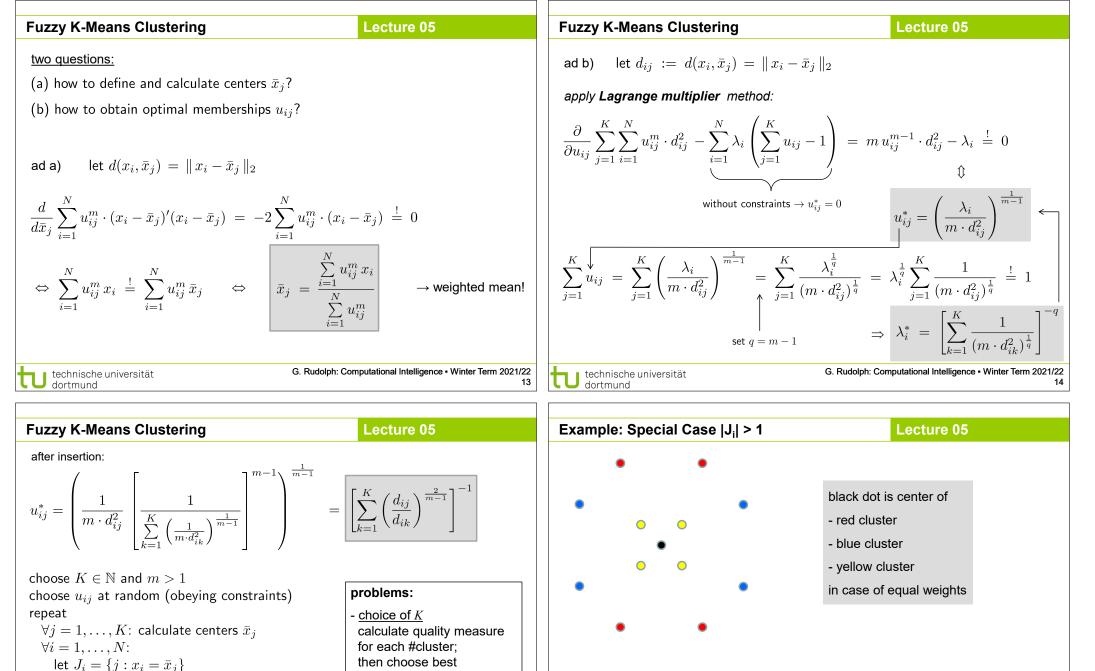
technische universität dortmund		Plan for Today Lecture 05
<b>Computational Intel</b> Winter Term 2021/22	ligence	Fuzzy Clustering
Prof. Dr. Günter Rudolph Lehrstuhl für Algorithm Engineering (L Fakultät für Informatik TU Dortmund	S 11)	G. Rudolph: Computational Intelligence • Winter Term 202
Cluster Formation and Analysis	Lecture 05	Cluster Formation and Analysis Lecture 05
Introductory Example: Textile Industry → production of T-shirts (for men) $\downarrow$	best for producer ∶ one size vs. best for consumer: made-to-measure ⇒ compromize: S, M, L, XL, 2XL	<ul> <li>idea:</li> <li>select, say, 2000 men at random and measure their "body lengths"</li> <li>arrange these 2000 men into five disjoint groups</li> <li>such that <ul> <li>deviations from mean of group as small as possible</li> <li>differences between group means as large as possible</li> </ul> </li> </ul>
	$^{\gamma}$ 5 sizes $\rightarrow$ OK, but which lengths for which size?	<ul> <li>in general:</li> <li>arrange objects into groups / clusters</li> <li>such that <ul> <li>elements within a cluster are as homogeneous as possible</li> <li>elements across clusters are as heterogeneous as possible</li> </ul> </li> </ul>
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- choice of m

typical: *m*=2;

try some values;

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use interval  $\rightarrow$  fuzzy type-2

if  $J_i = \emptyset$  determine memberships  $u_{ij}$ 

until  $D(C^{(t)}) - D(C^{(t+1)}) < \varepsilon$  or  $t = t_{max}$ 

and  $u_{ij} = 0$  for  $j \notin J_i$ 

choose  $u_{ij}$  such that  $\sum_{j \in J_i} u_{ij} = 1$ 

else

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 $u_{ii} = 1 / |J_i|$  for  $j \in J_i$  appears plausible

but: different values algorithmically better

 $\rightarrow$  cluster centers more likely to separate again ( $\rightarrow$  tiny randomization?)

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Measures for Cluster QualityLecture 05• Partition Coefficient  
$$PC(C_1, \ldots, C_K) = \frac{1}{N} \sum_{i=1}^N \sum_{j=1}^K u_{ij}^2$$
 ("larger is better")  
maximum if  $u_{ij} \in \{0, 1\} \rightarrow crisp partitionminimum if  $u_{ij} = \frac{1}{K} \rightarrow entirely fuzzy$  $\frac{1}{K} \leq PC(C_1, \ldots, C_K) \leq 1$ • Partition Entropy  
 $PE(C_1, \ldots, C_K) = -\frac{1}{N} \sum_{i=1}^N \sum_{j=1}^K u_{ij} \cdot \log_2(u_{ij})$  ("smaller is better")  
maximum if  $u_{ij} = \frac{1}{K} \rightarrow entirely fuzzyminimum if  $u_{ij} \in \{0, 1\} \rightarrow crisp partition$  $0 \leq PE(C_1, \ldots, C_K) \leq \log_2(K)$ • Consider universitit  
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